



ISSN: 2350-0328

**International Journal of Advanced Research in Science,
Engineering and Technology**

Vol. 8, Issue 2 , February 2021

Adaptive Fuzzy Control System for Multi-Dimensional Dynamic Object under the Conditions of Uncertainty of Information

D.A.Khalmatov, U.O.Khuzhanazarov, G.R.Alimova, J.M.Murodov

Assistant professor, Department of Automation and management of industrial and technological processes, Tashkent Institute of textile and light industry Tashkent, Uzbekistan

Senior Lecturer, Department of Automation and management of industrial and technological processes, Tashkent Institute of textile and light industry Tashkent, Uzbekistan

Doctoral student, Department Information processing and management system, Tashkent State Technical University, Tashkent, Uzbekistan

Senior Lecturer, Department of Automation and management of industrial and technological processes, Tashkent Institute of textile and light industry Tashkent, Uzbekistan

ABSTRACT: A mathematical model of dynamic objects in the state space under conditions of fuzzy initial information is proposed. An adaptive-fuzzy control algorithm for technological objects is synthesized based on a dynamic model with robust properties. To impart robustness to the control algorithm, it is proposed to use a discrete velocity gradient algorithm in a parametric form, which will provide a minimum of complexity and take into account the constraints on the control signal and its rate of change. The proposed algorithm was implemented to control the processes in the rectification plant, which allowed a decrease in the transient process by 20% and the deviation of the vector of state variables from the reference one by 15%.

KEY WORDS: Mathematical model, adaptive system, modeling, algorithm, robustness, state spaces

I. INTRODUCTION

Modern technological objects are complex weakly formalized systems operating under conditions of great uncertainty, incomplete knowledge and unclear descriptions of both the system itself and the disturbances acting on it. To manage such objects, it is not enough to use classical methods of control theory, and there is a need to develop new methods and approaches using the achievements of modern information technologies. One of these approaches, based on the theory of fuzzy sets and fuzzy logic, is the basis for the creation of an intellectualized control system for technological objects operating under conditions of information uncertainty.

In this case, in order to increase the efficiency of managing technological objects using modern management methods, it is necessary to solve the following tasks:

- assessment of quality indicators of uncertainty
- reduction (or compensation) of a priori uncertainty of knowledge about the process due to the use of operational information from measuring instruments and construction of an adaptation loop
- the formation of such a control law that would guarantee stability and specified indicators of accuracy and quality of the control system (CS) in conditions of uncompensated (a posteriori) uncertainty.

II. METHODOLOGY

One of the possible ways to solve these problems is the use of methods of adaptive, robust and fuzzy control [1, 2].

An important point in this case is the construction of a mathematical model for representing knowledge about dynamic objects in conditions of fuzzy information, which should make it possible to determine the uncertainty indicators, give a description of random processes, invariant to their distribution law.

- fuzzy equation of state

$$d\bar{x}/dt = \bar{A} \otimes \bar{x} \oplus \bar{B} \otimes u, \quad \mu_{\bar{S}}(s), \tag{1}$$

- fuzzy observation equation

$$\bar{y} = \bar{C} \otimes \bar{x}, \tag{2}$$

- fuzzy initial conditions

$$\bar{x}_1(0) = \bar{D}_1, \bar{x}_2(0) = \bar{D}_2, \dots, \bar{x}_n(0) = \bar{D}_n, \tag{3}$$

where \otimes, \oplus - fuzzy operations, respectively, addition and multiplication; u - control signal (scalar) that takes fuzzy values; $\bar{x} = \{\bar{x}_1, \bar{x}_2, \dots, \bar{x}_i, \dots, \bar{x}_n\}$ - a vector of a fuzzy state, $i = 1, 2, \dots, n$; $\bar{y} = \{\bar{y}_1, \bar{y}_2, \dots, \bar{y}_\zeta, \dots, \bar{y}_l\}$ - a vector of fuzzy output variables, $\zeta = 1, 2, \dots, l$; $\mu_{\bar{S}}(s)$ - indicator of a fuzzy (changing) number of state variables and representing the weight of the s -th equation of state;

$$\bar{A} = \begin{bmatrix} \bar{A}_1^1 & \dots & \bar{A}_n^1 \\ \dots & \dots & \dots \\ \bar{A}_1^n & \dots & \bar{A}_n^n \end{bmatrix}, \bar{B} = \begin{bmatrix} \bar{B}^1 \\ \dots \\ \bar{B}^n \end{bmatrix}, \bar{C} = \begin{bmatrix} \bar{C}_1^1 & \dots & \bar{C}_n^1 \\ \dots & \dots & \dots \\ \bar{C}_1^l & \dots & \bar{C}_n^l \end{bmatrix} - \text{matrix of fuzzy coefficients of the model.}$$

Some i -th variable of the state vector as a function of time t can be represented by a fuzzy relation (FR) [3,4]: $\bar{x}_i(t) = \{t, x_i / \mu_{\bar{x}_i}^-(t, x_i)\}$, $i = 1, 2, \dots, n$, and at a fixed moment in time, this variable can be expressed by a fuzzy set (FS): $\bar{x}_i = \{x_i / \mu_{\bar{x}_i}^-(x_i)\}$. The ζ -th output variable has a similar description:

$$\bar{y}_\zeta(t) = \{t, y_\zeta / \mu_{\bar{y}_\zeta}^-(t, y_\zeta)\}, \zeta = 1, 2, \dots, l,$$

$$\bar{y}_\zeta = \{y_\zeta / \mu_{\bar{y}_\zeta}^-(y_\zeta)\},$$

where $\mu_{\bar{x}_i}^-, \mu_{\bar{y}_\zeta}^-$ are membership functions (MF); x_i, y_ζ - values from universal sets. Matrix elements $\bar{A}, \bar{B}, \bar{C}$ are given by the FS:

$$\bar{A}_1^1 = \{A_1^1 / \mu_{\bar{A}_1^1}^-(A_1^1)\}, \dots, \bar{A}_n^n = \{A_n^n / \mu_{\bar{A}_n^n}^-(A_n^n)\},$$

$$\bar{B}^1 = \{B^1 / \mu_{\bar{B}^1}^-(B^1)\}, \dots, \bar{B}^n = \{B^n / \mu_{\bar{B}^n}^-(B^n)\},$$

$$\bar{C}_1^1 = \{C_1^1 / \mu_{\bar{C}_1^1}^-(C_1^1)\}, \dots, \bar{C}_n^l = \{C_n^l / \mu_{\bar{C}_n^l}^-(C_n^l)\}.$$

The initial conditions are described by the FS $\bar{D}_i = \{x_i / \mu_{\bar{D}_i}^-(x_i)\}$, and the number of state vector variables is described by - the FS $\bar{S} = \{s / \mu_{\bar{S}}^-(s)\}$, where $s = 1, 2, \dots, n$ is the ordinal number of the state vector variable.

Membership functions are specified by analytical dependence [2], for example, for a variable \bar{x}_i :

$$\mu_{\bar{x}_i}^-(x_i) = \varphi(x, a_{\bar{x}_i}, b_{1\bar{x}_i}, b_{2\bar{x}_i}, v_{1\bar{x}_i}, v_{2\bar{x}_i}) =$$

$$= \left((b_{1\bar{x}_i}(a_{\bar{x}_i} - x))^{v_{1\bar{x}_i}} \frac{\text{sign}(b_{1\bar{x}_i}(a_{\bar{x}_i} - x)) + 1}{2} + (b_{2\bar{x}_i}(a_{\bar{x}_i} - x))^{v_{2\bar{x}_i}} \frac{\text{sign}(b_{2\bar{x}_i}(a_{\bar{x}_i} - x)) + 1}{2} + 1 \right)^{-1} \tag{4}$$

In formula (4), the coefficient $a_{\bar{x}_i}$ represents the MF mode, the coefficients $b_{1\bar{x}_i}$ and $b_{2\bar{x}_i}$ set the MF width, $v_{1\bar{x}_i}$ and $v_{2\bar{x}_i}$ is the slope of the MF to the x_i axis, i.e. contrast. Coefficients $b_{1\bar{x}_i}, b_{2\bar{x}_i}, v_{1\bar{x}_i}, v_{2\bar{x}_i}$ allow to form any form of MF and can act as indicators of uncertainty.

The quality indicators of the control system (transient time, overshoot, tracking error, etc.) are set in the form of utility functions:

$$\begin{aligned} \bar{Q}_k^3 &= \left\{ Q_k^3 / \mu_{Q_k^3}^3(Q_k^3) \right\}, k = 1, 2, \dots, K, \\ \mu_{Q_k^3}^3(Q_k^3) &= \phi(Q_k^3, a_{\bar{x}_i}^3, b_{1\bar{x}_i}^3, b_{2\bar{x}_i}^3, v_{1\bar{x}_i}^3, v_{2\bar{x}_i}^3), \end{aligned} \tag{5}$$

where K - is the number of quality indicators of the control system.

A reference model was determined based on the specified indicators of management quality:

$$\dot{x}_m = A_m x_m + B_m u_m, \tag{6}$$

where u_m - is the setting action of the system; $x_m(t)$ - vector of reference states.

Constraints on the variables of the state vector and constraints on control are set;

$$\begin{aligned} g_1(\bar{x}, u, \gamma, t) &< x_{1\max}, g_2(\bar{x}, u, \gamma, t) < x_{2\min}, \dots, \\ g_{2n-1}(\bar{x}, u, \gamma, t) &< x_{n\max}, g_{2n}(\bar{x}, u, \gamma, t) < x_{n\min}, \dots, \\ g_{m-1}(\bar{x}, u, \gamma, t) &< u_{\max}, g_m(\bar{x}, u, \gamma, t) < u_{\min}. \end{aligned} \tag{7}$$

Let the minimization of the average deviation of the state vector variables of the real behavior of the controlled object from the standard be chosen as the control goal.

It is necessary to synthesize control systems and adjust the regulator so that all signals to the control systems are limited, i.e. $|x(t)| < x_{add}, |u(t)| < u_{add}$, and the transient processes in the system met the specified quality indicators (5).

To determine the quality indicator of the control system $a_{x_i}^-(t), a_{y_i}^-(t)$, both the time characteristics of the control object and the fuzzy parameters $b_{1x_i}^-(t), b_{2x_i}^-(t), b_{1y_k}^-(t), b_{2y_k}^-(t)$, are used, determined by the width of the membership function.

In order to reduce the ambiguity of the data about the object and improve the control quality indicators, the values $b_{1x_i}^-(t), b_{2x_i}^-(t), b_{1y_k}^-(t), b_{2y_k}^-(t)$.

To impart robustness to the control algorithm, it is proposed to use a discrete velocity gradient algorithm in a parametric form, which will provide a minimum of complexity and take into account the constraints on the control signal and the rate of its change [5-9].

In this case, the control signal is formed on the basis of a fuzzy set of values of state variables, which is possible when the behavior of the object is varied.

Due to the fact that the object model is an averaging summation filter, the synthesis of the control law based on the fuzzy model additionally enhances the robustness of the velocity gradient algorithm, while maintaining the boundedness of phase trajectories in a certain area under conditions of uncompensated uncertainty of values about the object.

In order to improve the quality and accuracy of the formation of transient processes in control systems, an algorithm for making decisions on the choice of a compromise control signal by embedding it in control algorithms is implemented.

The modified control law is as follows:

$$u = k_u(t) \cdot u_m(t) + \sum_{i=1}^n k_x^\Sigma(t) \cdot x_i^\Sigma(t), \tag{8}$$

$$k_{x1}^\Sigma[t+1] = k_{x1}^\Sigma[k](1 - h\gamma_3) + h(\gamma_5 - \gamma_4)\delta \cdot [t]x_1^\Sigma[t] - h\gamma_5\delta \cdot [t+1]x_1^\Sigma[t+1], \tag{9}$$

$$k_{xn}^\Sigma[t+1] = k_{xn}^\Sigma[k](1 - h\gamma_3) + h(\gamma_5 - \gamma_4)\delta \cdot [t]x_n^\Sigma[t] - h\gamma_5\delta \cdot [t+1]x_n^\Sigma[t+1], \tag{10}$$

$$k_u[t+1] = k_u[k](1 - h\gamma_1) + h(\gamma_6 - \gamma_2)\delta \cdot [t]u_m[t] - h\gamma_6\delta \cdot [t+1]u_m[t+1], \tag{11}$$

where $t = mh$, $h > 0$ is the sampling step, $m = 0, 1, 2, \dots, m$; $\gamma = \{\gamma_1, \gamma_2, \gamma_3, \gamma_4, \gamma_5, \gamma_6\}$ - parameters of the adaptive controller; $e_i^\Sigma = \int_{X_i} (x_i - x_{im}) \mu_{e_i}^-(e_i) dx_i$ - mismatch between state vector variables and reference state variables;

$\mu_{e_i}^-(e^i) = (e_i, a_{e_i}^-, b_{1e_i}^-, b_{2e_i}^-, v_{1e_i}^-, v_{2e_i}^-)$ - MF of the error, φ - is the analytical form of the membership function in the form (4), $a_{e_i}^- = a_{xi}^- - x_{im}$, $v_{1e_i}^- = v_{1xi}^-$, $v_{2e_i}^- = v_{2xi}^-$, $b_{1e_i}^- = b_{1xi}^-$, $b_{2e_i}^- = b_{2xi}^-$, $x_i^\Sigma = \int_{X_i} x_i dx_i$ - is the

integrated variable of the state vector; $\delta \cdot [t] = \sum_{i=1}^n k_i \cdot e_i^\Sigma$, h_i - are the coefficients obtained from the coefficients of the matrix and the solution of the Lyapunov equation and the matrix of the reference model B_m .

The problem of determining the parameters of an adaptive controller $\gamma = \{\gamma_1, \gamma_2, \gamma_3, \gamma_4, \gamma_5, \gamma_6\}$, when the quality indicators of the control system (5) and the behavior of the control object (1), (2), (3) are given in a fuzzy form, can be reduced to the classical clear problem of finding the extremum of the objective function in the presence of constraints (7)

For this, a generalized criterion is proposed, which, firstly, combines the quality indicators of the control system, and secondly, implements defuzzification of fuzzy values of the quality indicator of the control system:

$$I(\gamma) = K - \sum_{k=1}^K \frac{\mu_{Q_k}^{\int} \wedge \mu_{Q_k}^{\int 3}}{\mu_{Q_k}^{\int}} \rightarrow \min, \tag{12}$$

where $\mu_{Q_k}^{\int} = \int_{-\infty}^{\infty} \mu_{Q_k}^-(Q_k) \cdot dQ_k$ - is the energy of the FS $\bar{Q}_k = \{Q_k / \mu_{Q_k}^-(Q_k)\}$ expressing the value of the k -th

quality indicator of the control system predicted on the basis of the fuzzy model; $\mu_{Q_k}^{\int 3} = \int_{-\infty}^{\infty} \mu_{Q_k}^3(Q_k^3) \cdot dQ_k^3$ - energy of FS, expressing the utility function.



ISSN: 2350-0328

International Journal of Advanced Research in Science, Engineering and Technology

Vol. 8, Issue 2 , February 2021

III.CONCLUSION

The study of the effectiveness of the proposed approach in the operation of a fuzzy adaptive system was carried out with temperature and level control in a rectification unit [1].

The following results were obtained:

- 1.Operational formation of control signals helps to reduce the time of the transient process by 20%.
 2. The average deviation of the vector of the state variables of the real process from the reference one is reduced by 15% in comparison with the indicators of the known adaptive control systems.
- The implementation of the proposed control system synthesis algorithm expands the area of application of control systems in production conditions in the presence of a wide range of disturbances.

REFERENCES

- [1].Kudinov Yu. I., Dorokhov IN Control of a rectification plant based on fuzzy sets // Theoretical foundations of chemical technology. - 1991. - T. 25, No. 4. - from. 563-569.
- [2].Siddikov I.X., Umurzakova D.M. Fuzzy-logical Control Models of Nonlinear Dynamic Objects // Advances in Science, Technology and Engineering Systems Journal, Vol. 5, No. 4, 419-423 (2020). DOI: 10.25046/aj050449.
- [3].SiddikovI.Kh., Khalmatov D.A., Khuzhanazarov U.O., Alimova G.R. System of Analytical Control and Control of Technological Parameters of Cotton-Cleaning Production // International scientific and technical journal "Chemical technology. Control and management".2020, №5-6 (95-96), P.134-139
- [4].Halmatov D.A., Yunusova S.T., Atajonov M.O., Huzanazarov U.O. Formalization of the cotton drying process based on heat and mass transfer equations//IIUM Engineering Journal, Vol. 21, No. 2, 2020. P.256-265. <https://doi.org/10.31436/iiumej.v21i2.1456>
- [5]. Methods of robust, neuro-fuzzy and adaptive control / Ed. Egupova. M. : Moscow State Technical University named after N.E.Bauman, 2002.- 744p.
- [6].Miroshnik IV, Nikiforov VO, Fradkov AL Nonlinear and adaptive control of complex dynamic systems. SPb. : Nauka, 2000. -549s.
- [7].IgamberdievKh.Z., Yusupbekov A.N., Zaripov O.O. Regular methods for assessing and managing dynamic objects under conditions of uncertainty. Tashkent. : Publishing house of Tashkent State Technical University, 2012.-320s.
- [8].Siddikov I.H. Synthesis of Neuro-Fuzzy controller for dynamic objects under conditions of uncertainty // The Advanced Science Journal, USA, Volume 2014 Issue 2. pp. 33-37
- [9].SidikovI.X., Kamalov N.Z., Khalmatov D.A., Khujanazarov U.O. Automatic control process for drying a cotton on the basis of fuzzy logic// International Journal of Advanced Research in Science, Engineering and Technology. Vol. 6, Issue 10, October 2019. p. 11093-11096



ISSN: 2350-0328

**International Journal of Advanced Research in Science,
Engineering and Technology**

Vol. 8, Issue 2 , February 2021

AUTHOR'S BIOGRAPHY



Khalmatov Davronbek Assistant professor, Department of Automation and Control of Technological Processes and Production, Tashkent Institute of Textile and light industry, Tashkent, Uzbekistan



Khuzhanazarov Ulugbek Senior lecturer, Department of Automation and Control of Technological Processes and Production, Tashkent Institute of Textile and light industry, Tashkent, Uzbekistan



Alimova Gulchehra Doctoral student, Department of Information processing and management system of faculty Electronics and Automatics, Tashkent State Technical University, Tashkent, Uzbekistan



Murodov Jurabek Senior lecturer, Department of Automation and Control of Technological Processes and Production, Tashkent Institute of Textile and light industry, Tashkent, Uzbekistan